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# Section 1 INTRODUCTION TO PERCENTS

A percentage is one way to express a fraction. If you set a goal to read 10 pages in a book, after you have read 5 of them, you have finished 5 out of 10, or five-tenths of your goal. Using percentage language, you can say you have read 50 percent (50%) of your goal.

1. To learn the topics in this book, you should already be familiar with some percentage concepts. For example, you should know how to write a fraction as a percent.

Without a calculator, how can you convert  $\frac{1}{5}$  to a percent?

2. When it is difficult to convert a fraction to a percent, it is likely a better use of your time to use a calculator to do the conversion.

Using a calculator, how can you convert  $\frac{19}{40}$  to a percent?

3. What portion of the figure is shaded in each image below? Express this as a simplified fraction.

a.



b.



c.



d.



4. Convert each of the previous fractions to percents.

5. When you calculate a percent of another number, like 10% of 200, you identify a specific fractional amount of that number. Some percents are easier to compute. For example, what is 50% of 10?

		OUIDED DIOU	UVLIII UULIVAIIIUU		
	percentages are more iar with common perce		still be computed with	out a calculator if you are	
	a. How much mone	ey is 25% of \$4?			
		• •	orchard and you used did you have left over:	75% of the apples to make	
quick			•	me and can be done more calculator is only helpful if	
			making a calculator coesult is not reasonable.	ompute 50x10, the calculat	or
	can estimate percenta kes. Try to estimate e			otice your errors if you mak	(e
	a. 48% of 12	b. 26% o	f 16 c	. 99.1% of 20	
			nple, 300% of 20 mean s 3 sets of 20, which is	s 3 sets of "100% of 20." 60.	
9. Use a	calculator to compute	e 364% of 45.			
22% d multi	of N, or even smaller a	s 0.22N. The expression of the percent by the	on $0.22N$ shows that your variable $N$ . Write an	r" in a smaller format, such ou can compute 22% of <i>N</i> b expression that represents	У
	a. 50% of <i>A</i>	b. 3% of <i>B</i>	c. 275% of C	d. 0.4% of <i>D</i>	

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Now that you have reviewed some percentage topics, this book will build on these topics and guide you through a selection of scenarios that use percents to make comparisons and calculations.



Use this page to record important ideas in the previous section or for any other writing that helps you learn the topics in this book.

## Section 2 PERCENT CHANGES: INCREASES & DECREASES

11.	A puffer fish has a circumference of 10 inches. When it feels threatened, it sucks in water and increases its circumference to 15 inches. To show a numerical change like this, you can compare the amount of the increase to the original amount. The fish grows by 5 inches, which is% of its original circumference. Using percents, the circumference grows by%.
12.	If the fish continues to feel threatened, it expands its body more, until its circumference is 20 inches. Since the fish has now expanded by a total of 10 inches, it has increased its <u>original</u> circumference by%. This shows an interesting detail. If a number increases to become twice as large as its original value, it has increased by%.
13.	If a number becomes three times as large as its initial value, by what percent has it increased?
14.	If a number becomes one fourth of its original value, by what percent has it decreased?
15.	Suppose that you measure your height one year and find that you are 50 inches tall. One year later, you measure again to check your growth and you find that your height has increased to 54 inches. In order to describe your growth as a percent increase you need to first consider your amount of growth which is 4 inches.
	a. The <u>amount</u> of growth is a fractional amount of your original height, in this case $\frac{4}{50}$ . This fraction can be simplified and written as the fraction
	b. Every fraction can be represented in decimal form. Use a calculator to write the value of $\frac{2}{25}$ in its decimal form.
	c. If you express 0.08 as a percent, it is%, which leads us back to the height scenario above. If your height increases from 50 inches to 54 inches, you can say that your height has increased by%.
16.	Your height increases from 54 inches to 58 inches during the next year, another yearly increase of 4 inches. Does this represent an 8% increase again? If not, by what percent did your height increase if it changed from 54 to 58 inches?

	The previous scenario involves challenging numbers. Return to simpler numbers for a moment in order to gain more familiarity with percentage changes.
17.	A shirt initially costs \$50, but it goes on sale for \$40. Its price was decreased by%.
18.	There are 80 students who are absent on Monday, and 100 students are absent on Tuesday. From Monday to Tuesday, the number of absences increased by%.
19.	An \$80 pair of boots decreases by \$20 to sell for \$60. A pair of shoes is priced at \$60, but it only sells for \$40. Which item had its price reduced by a greater percent, the boots or the shoes?
20.	If 40 people earned a passing score last year, and only 20 people earned a passing score this year, by what percent did the number of passing scores decrease?
21.	If you owe \$20 to your friend today, and tomorrow you pay the entire amount that you owe, by what percent did you reduce the amount of money that you owed your friend?
22.	When 100 increases to become 140, it might be easy for you to see that 100 has increased by 40 percent, because 100 is an easy number to work with. The number 100 is the foundation of percentages. The word percent comes from the phrase "per cent," which means "per 100." Try something more challenging to see if you understand the concept of percent change. If \$140 increases to become \$180, by what percent has it increased?
23.	Fill in each blank below.
	a. If 100 increases by 20%, its new value is
	b. If 100 decreases by 20%, its new value is
	c. If 80 increases by 35%, its new value is
	d. If 80 decreases by 35%, its new value is

## Section 3 WRITING EQUATIONS TO CALCULATE PERCENTS

In this section, you will learn how to write equations to solve percent scenarios.

35.	Write each	n statement as an equation, but do not solve	the equation.
	a.	The product of a number and 5 is 20.	
	b.	The quotient of 100 and a number is 50.	
	C.	6 is 7 less than 3 times a number.	
36.	Write each	n statement as an equation, but do not solve	the equation.
	a.	A number is 3 more than 10.	b. A number is 6 less than 4.
	C.	3 is 4 more than a number.	d. A number increased by 5 is 15.
	-	· · · · · · · · · · · · · · · · · · ·	, but they are intended to help you think about ext scenarios will focus only on percentages.
37.	Write each	n statement as an equation. Do not solve th	e equation.
	a.	50% of a number is 45.	
	b.	A number is 24% of 80.	
	C.	15 is a percentage of 20.	
38.	easier to w		t is difficult to mentally compute this, but it is tatement into an equation: "A number is 45%

### Section 10 **ANSWER KEY**

	Other options exist, but one way is to		
	change the denominator to 100. This makes		
	it easy to state the fraction as a percent.		
1.	,		
	$\frac{1}{5} \cdot \frac{20}{20} \rightarrow \frac{20}{100}$ "20 hundredths" is 20 per 100		
	which has the same meaning as 20%.  Find the decimal form of the fraction. In the		
	calculator, divide 19 by 40. To do this, input 19÷40 or 19/40. As a decimal, 19/40 is		
	0.475, which is 475 thousandths or 47.5		
2.	hundredths. 47.5 per 100 is 47.5 percent		
۷.	(47.5%). You may have learned to move the		
	decimal 2 places to the right to convert a		
	decimal to a percent, and this is true but it is		
	important to know why that works.		
	,		
3.	a. $\frac{3}{4}$ b. $\frac{3}{6} \rightarrow \frac{1}{2}$ c. $\frac{3}{8}$ d. $\frac{3}{10}$ a. 75% b. 50% c. 37.5% d. 30%		
	4 6 2 8 10 a. 75% b. 50% c. 37.5% d. 30%		
4.			
5.	One-half of 10, which is 5.		
6.	a. \$1 b. 5 pounds (75% of 20 is 15)		
	500; 50% of a number is one-half of that		
7.	number. One-half of 10 is just 5, so a result		
	of 500 is not reasonable.		
0	a. ≈6 (about 50% of 12)		
8.	b. ≈4 (about 25% of 16)		
	c. ≈20 (about 100% of 20)		
9.	$3.64 \times 45 \rightarrow 163.8$ a. 0.5A b. 0.03B c. 2.75C d. 0.004D		
10.			
11.	50%		
12.	100%		
13.	200%		
14.	75%		
15.	a. $\frac{2}{25}$ b. 0.08 c. 8		
16.	Approx. 7.4% $\left(\frac{4}{54} \text{ is } 0.\overline{074} \text{ in decimal form}\right)$		
17.	20%		
18.	25%		
19.	the shoes $\left(33\frac{1}{3}\% \text{ vs. } 25\%\right)$		

20.	50%		
21.	100%		
22.	$\frac{40}{140}$ $\rightarrow$ 0.286 $\rightarrow$ approx. 28.6%		
23.	a. 120 b. 80 c. 108 d. 52		
24.	a. E + 0.5E b. F - 0.25F		
25.	a. 1.5E b. 0.75F c. 1.05G d. 0.85H		
26.	a. 1.35X - b. 0.81X - c. 2X - d. 0		
27.	a. 170 b. 75 a. 20% (increase) b. 10% (decrease)		
28.	c. 80% (decrease)		
29.	a. 120% (increase) b. 200% (increase) c. 350% (increase)		
30.	72% (decrease)		
31.	a. increase 64% b. increase 150% c. decrease 1% d. increase 400%		
32.	$\frac{259}{490} \rightarrow 0.529 \rightarrow \text{approx. } 52.9\%$		
33.	$\frac{253}{30} \rightarrow 8.43 \xrightarrow{-} 843\frac{1}{3}\%$		
34.	Between June and July (20.7% increase)		
35.	a. $5n = 20$ b. $100 \div n = 50$ c. $6 = 3n - 7$		
36.	a. $n = 10 + 3$ b. $n = 4 - 6$ c. $3 = n + 4$ d. $n + 5 = 15$ a. $0.5n = 45$ b. $n = 0.24(80)$		
37.	a. $0.5n = 45$ b. $n = 0.24(80)$ c. $15 = \frac{n}{100}(20)$ or $15 = n(20) \rightarrow \text{if } n \text{ is the}$ decimal form of the percentage.		
38.	n = 0.45(18)		
39.	a. X = 0.12(30) b. 0.12(30) = X c. 45 = 0.2X d. 0.2X = 45		
40.	a,b. 3.6 c,d. 225		
41.	a. $18 = \frac{x}{100} (24)$ b. $\frac{x}{100} (24) = 18$		
	c. $36 = \frac{x}{100} (15)$ d. $\frac{x}{100} (15) = 36$		
42.	a, b. 75% c, d. 240%		
43.	a. 45% of 200 is $B \rightarrow 0.45(200) = B$ b. 65% of F is $70 \rightarrow 0.65F = 70$		